

# Numerical and Experimental Investigation of Laminar One-Dimensional Counter-Flow Flames Using Product Gas From Pyrolysis and Gasification of Woody Biomass

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## Abstract

Further advances in the utilization of biomass-based gaseous fuels in combustion systems require a deeper understanding of the combustion chemistry behind, as well as of the coupling of the chemistry with physical phenomena such as turbulence. The former is investigated in the present study combining both experiments with numerical simulations of different types of laminar non-premixed flames (sooting and non-sooting) in a counter-flow setup. The focus is put on synthetic gas mixtures, resembling, to different extents, typical compositions of the product gas obtained in biomass gasification consisting of CH<sub>4</sub> (reference) and CH<sub>4</sub> mixed with CO<sub>2</sub>, N<sub>2</sub>, O<sub>2</sub>, and/or H<sub>2</sub>, always. The oxidizer in all cases is air. A wide range of air-fuel ratios is considered. The influence of the product gas composition on the flame behaviour and flame structure with respect to the changes of the species profiles and peak temperatures with changing flow velocities is discussed. Laser-based spectroscopy techniques, in particular laser-induced Rayleigh scattering and laser-induced fluorescence (LIF), are applied as diagnostic tools. The former can provide an accurate understanding of temperature distributions, while the latter helps to identify the flame front through the tracking of intermediate species, such as CH<sub>2</sub>O (formaldehyde). Additionally, CH\* chemiluminescence contributes to localize the flame front. Lastly, the influence of the N<sub>2</sub>-shroud flow velocities and diameters, as well as resulting buoyancy effects due to a raise in temperature, are taken into account. In correspondence to these experiments, the flames are numerically simulated by an in-house time-dependent implicit Fortran code.

## 1. Introduction

Thermochemical conversion is a promising alternative for decentralized energetic utilization of biomass and waste. In particular, processes such as pyrolysis and gasification offer the possibility to produce a fuel gas to be used, among other applications, in internal combustion engines or turbines as part of combined heat and power generation (CHP). However, these fuels are more complex than conventional gaseous fuels regarding their composition depending on the conversion process and conditions. Despite the low calorific value and possible low quality of biomass and organic residues, this feedstock has increased its appeal due to the essentially unlimited availability [1, 2]. The varying composition of the input materials and the wide range of possible process conditions do result

in significantly different product gas compositions. The subsequent combustion process has to deal with significant amounts of diluents like CO<sub>2</sub> and N<sub>2</sub>, next to combustible species like H<sub>2</sub>, CH<sub>4</sub> and CO [3]. In the present work the influence of the product gas composition on the flame behaviour and flame structure is addressed.

Investigation on syngas diffusion flames has been widely addressed in literature, with focus on the combustion of individual syngas components [4], hydrogen fuels [5] airstream dilution [6], the influence of primarily CO<sub>2</sub> dilution [7] or methane-air diffusion flames in a counter-flow setup [8]. In this study experiments and numerical simulation on laminar counter-flow diffusion flames are combined. The understanding of the combustion behaviour of these complex gaseous fuels in such flames is essential for the further application of the

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laminar flamelet model to describe turbulent combustion [8]. The flamelet model describes the flame front as a collective of individual laminar flame elements in a turbulent flow profile, providing an approach to describe these flames.

In the present study, the laminar diffusion flames were numerically simulated by an in-house implicit Fortran code [9], which solves the governing equations for total mass, mass fractions, momentum and energy for non-stationary laminar one-dimensional flames. In the simulations about 80 species were taken into account with a reaction mechanism of more than 500 elementary reversible reactions [10].

Regarding the experimental investigation, laser-induced Rayleigh scattering was applied to measure the temperature profile in the flame. This approach avoids potential perturbations of contact probes like thermocouples on the flame and contributes to a more accurate diagnosis. This is of special relevance in these investigations due to the impact of temperature on reaction rates and pollutant levels [11]. The Rayleigh intensity depends on the gas species scattering cross section and, therefore, also on the mixture fraction at each location in the flame. The cross section is temperature-dependant, being negatively correlated to temperature. This leads to different cross sections and hence scattering intensities in the flame profile in the wings and the centre of the flame.

This change in scattering intensity is shown in Fig. 1 for three flames excited at  $\lambda = 532$  nm, using three flow velocities ( $20 \text{ cm s}^{-1}$ ,  $40 \text{ cm s}^{-1}$  and  $60 \text{ cm s}^{-1}$ ) and the same fuel composition.

$\text{CH}_2\text{O}$  is an important intermediate species in combustion, typically used to investigate the flame structure. In the present work, laser-induced fluorescence is used as a non-intrusive technique to allow a sensitive detection of  $\text{CH}_2\text{O}$  with an excitation wavelength of  $\lambda = 355$  nm [12, 13].  $\text{CH}^*$  chemiluminescence is also used to locate the main

heat release zone in a flame [14]. In this study,  $\text{CH}^*$  chemiluminescence at  $\lambda = 430$  nm is collected to determine the spatial position of the flame between the two nozzles.

## 2. Experimental

A schematic of the experimental set-up is shown in Fig. 2. The burner system consists of two opposed nozzles, each 24.8 mm in diameter, with a varying separation distance. To achieve the compromise of having a stable laminar flame and also reducing the reflections induced by the laser light on the nozzles, an axial distance of 18.9 mm was used for all experiments presented here. The inner jets of oxidizer and fuel are both surrounded by an annular co-flow of  $\text{N}_2$  to avoid perturbations from ambient air and, therefore, ensure stabilization. By using a water-cooled heat exchanger at ambient temperature, the upper part of the burner assembly was cooled down.

The excitation wavelengths for laser-induced Rayleigh scattering ( $\lambda = 532$  nm) and laser-induced fluorescence of  $\text{CH}_2\text{O}$  ( $\lambda = 355$  nm) were generated by means of the second and third harmonics of a Quanta-Ray Lab pulsed Nd:YAG laser (Model: Lab150 by Spectra Physics, Santa Clara, USA). The laser beam was guided via periscopes into a focusing spherical lens, subsequently forming the beam into a thin collimated sheet (9 mm) by a combination of diverging and converging cylindrical lenses. The laser sheet entered the measurement region between the nozzles of the counter-flow burner, being imaged by an intensified CCD camera (Model: Nanostar by LaVision, Göttingen, Germany) positioned perpendicular to the laser sheet to collect the signal. By a linear response to the signal this ICCD is able to acquire and store hundreds of single shot images, using a chip size of  $1280 \times 1024$  pixels. The wavelength-specific

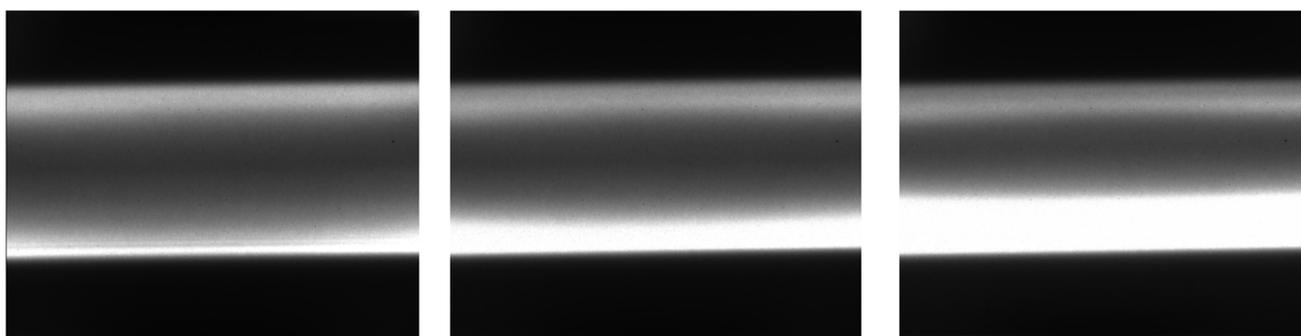


Fig. 1. Rayleigh signal (corresponding to temperature fields for diluted non-premixed  $\text{CH}_4 - \text{N}_2 - \text{CO}_2 - \text{air}$  flames (top: air side; bottom: fuel side); at velocities of  $20 \text{ cm s}^{-1}$ ,  $40 \text{ cm s}^{-1}$  and  $60 \text{ cm s}^{-1}$  (left to right)).

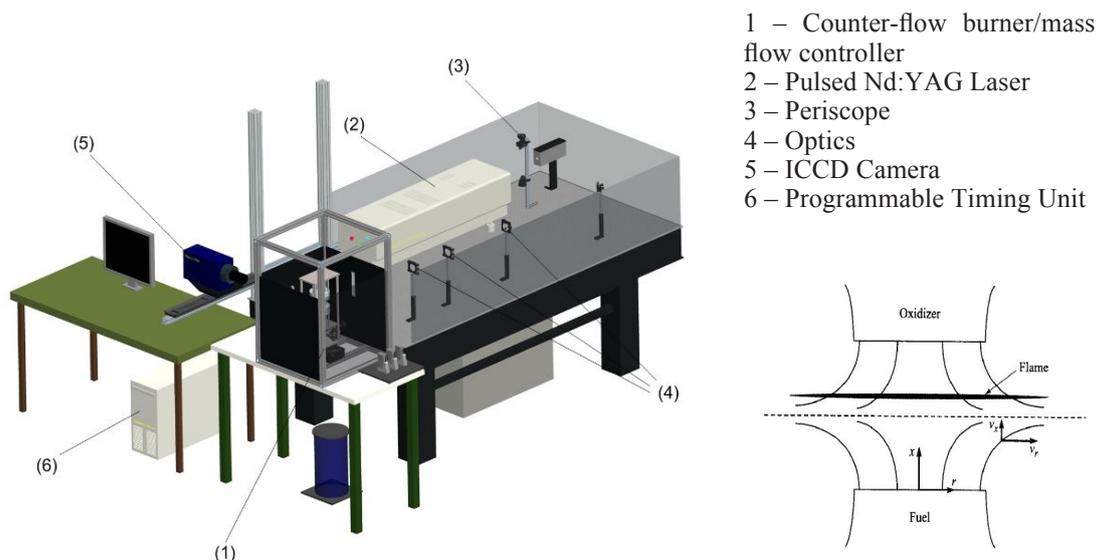


Fig. 2. Schematic of the experimental set-up (left) and counter flow flame (right) [15].

signals (scattering, fluorescence, chemiluminescence) was collected using BrightLine single-band bandpass (notch) filters, allowing only the respective wavelengths regions to pass through. All images obtained were corrected pulse by pulse via an energy monitor (Model: V9 dual head by LaVision, Göttingen, Germany) and for background scatter and variations in the laser sheet intensity.

Two compositions of gaseous fuel at velocities of  $20 \text{ cm s}^{-1}$ ,  $40 \text{ cm s}^{-1}$  and  $60 \text{ cm s}^{-1}$  were chosen for the experimental and numerical studies. Both fuel-side compositions contained 40% (volume)  $\text{CH}_4$  and 60% of diluent with the diluent being: a) 40%  $\text{CO}_2$  and 20%  $\text{N}_2$  or b) 20%  $\text{CO}_2$  and 40%  $\text{N}_2$ . Moreover, the addition of 5%  $\text{H}_2$  or up to 8%  $\text{O}_2$  to the fuel was investigated. The gases were mixed via mass-flow controllers (Model: red-y by

Vögtlin, Aesch, Switzerland). The gas mixtures are presented in Table 1.

In each study the experiments were conducted at identical velocities for the fuel- and oxidizer-sides. The flame is always located on the airside with respect to the stagnation plane. Increasing flow velocities, in the limit, leads to aerodynamic quenching of the flame. This extinction point can be identified by tracing the maximum temperature as function of the strain rate. The higher this critical strain rate, the higher its resilience to quenching, making the flame more stable for a wider range of flow conditions. That is desirable for an industrial combustion system, since the turn down ratio of the burner could be therefore increased, allowing a wider range of firing rates and thus enhancing the flexibility of the system.

**Table 1**  
Compositions of investigated fuels

Fuel composition	$\text{CH}_4$ [vol-%]	$\text{CO}_2$ [vol-%]	$\text{N}_2$ [vol-%]	$\text{H}_2$ [vol-%]	$\text{O}_2$ [vol-%]
Case A	40	40	20	-	-
Case A – $\text{H}_2$ addition	38	38	19	5	-
Case A – $\text{O}_2$ addition	39.2	39.2	19.6	-	2
Case A – $\text{O}_2$ addition	38.4	38.4	19.2	-	4
Case A – $\text{O}_2$ addition	37.6	37.6	18.8	-	6
Case A – $\text{O}_2$ addition	36.8	36.8	18.4	-	8
Case B	40	20	40	-	-
Case B – $\text{H}_2$ addition	38	19	38	5	-
Case B – $\text{O}_2$ addition	39.2	19.6	39.2	-	2
Case B – $\text{O}_2$ addition	38.4	19.2	38.4	-	4
Case B – $\text{O}_2$ addition	37.6	18.8	37.6	-	6
Case B – $\text{O}_2$ addition	36.8	18.4	36.8	-	8

The total Rayleigh scattering signal collected by a detector can be written as follows [11]

$$S = \eta I N V \int_{\Delta\Omega} \left( \frac{\delta\sigma}{\delta\Omega} \right)_{\text{mix}} \delta\Omega \quad (1)$$

where  $V$  is the observation volume,  $N$  the number density,  $I$  the incident laser intensity,  $\eta$  the optical collection efficiency,  $(\delta\sigma/\delta\Omega)_{\text{mix}}$  the differential scattering cross section of the gas mixture and  $\Delta\Omega$  the solid angle subtended by the collection optics. For a single molecular species at a specific wavelength the total Rayleigh scattering cross section can be written as follows [10]

$$\sigma(\lambda) = \frac{24\pi^3}{\lambda^4 N^2} \left( \frac{n(\lambda)^2 - 1}{n(\lambda)^2 + 2} \right)^2 \left( \frac{6 + 3\rho_0(\lambda)}{6 - 7\rho_0(\lambda)} \right) \quad (2)$$

where  $N$  is the number density,  $n(\lambda)$  is the refractive index and  $\rho_0(\lambda)$  is the depolarization ratio. Our approach to analysis follows that of Connelly et al. [16] where the directly measured Rayleigh scattering is compared with a model of the Rayleigh scattering rather than an interpolation of the Rayleigh

to estimate temperature or density that introduces errors which cannot be easily quantified [16]. Furthermore, based on the simulated species profiles and the incorporation of the scattering Rayleigh cross sections of the major species, together with the imaging systems possible point spread function to minimize crosstalk background phenomena, a good fit between model and experiment can be established. All contributions to background arising from scattering and the point spread function of the CCD need therefore to be included when analysing the experimental measurements and comparing them with the numerical results of the corresponding flames and vice versa [16].

### 3. Results

The numerical and experimental results regarding the Rayleigh scattering and subsequently extracted temperature curves (based on [11]) at fuel side variations of 40% CH<sub>4</sub> and a diluent distribution of either 40% CO<sub>2</sub> and 20% N<sub>2</sub> (case A) or 20% CO<sub>2</sub> and 40% N<sub>2</sub> (case B) at velocities of 20 cm s<sup>-1</sup> and 60 cm s<sup>-1</sup> are shown in Fig. 3.

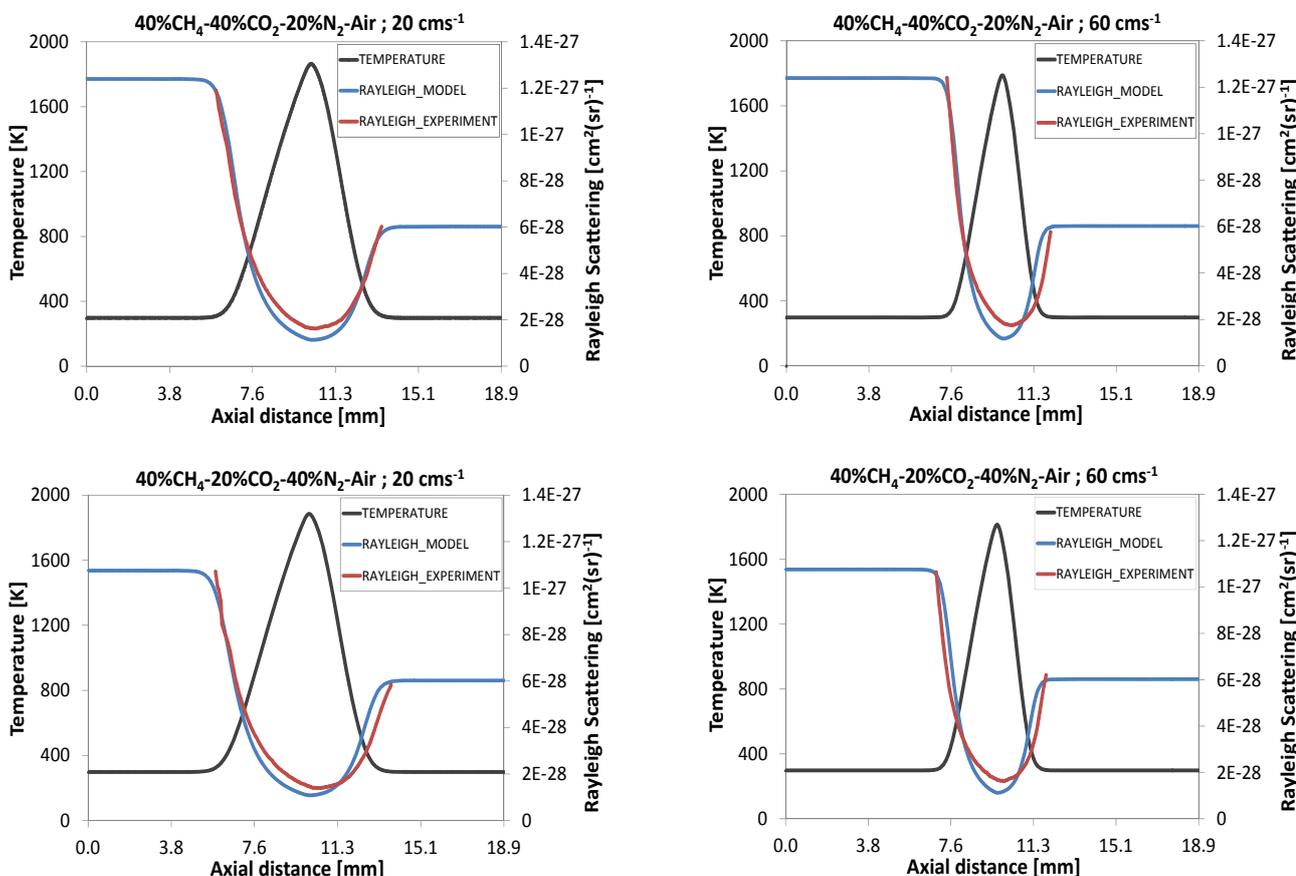


Fig. 3. Experimental and numerical solutions for 40% CH<sub>4</sub> – 40% CO<sub>2</sub> – 20% N<sub>2</sub> – air (case A) at 20 cm s<sup>-1</sup> (top left) and 60 cm s<sup>-1</sup> (top right); 40% CH<sub>4</sub> – 20% CO<sub>2</sub> – 40% N<sub>2</sub> – air (case B) at 20 cm s<sup>-1</sup> (bottom left) and 60 cm s<sup>-1</sup> (bottom right).

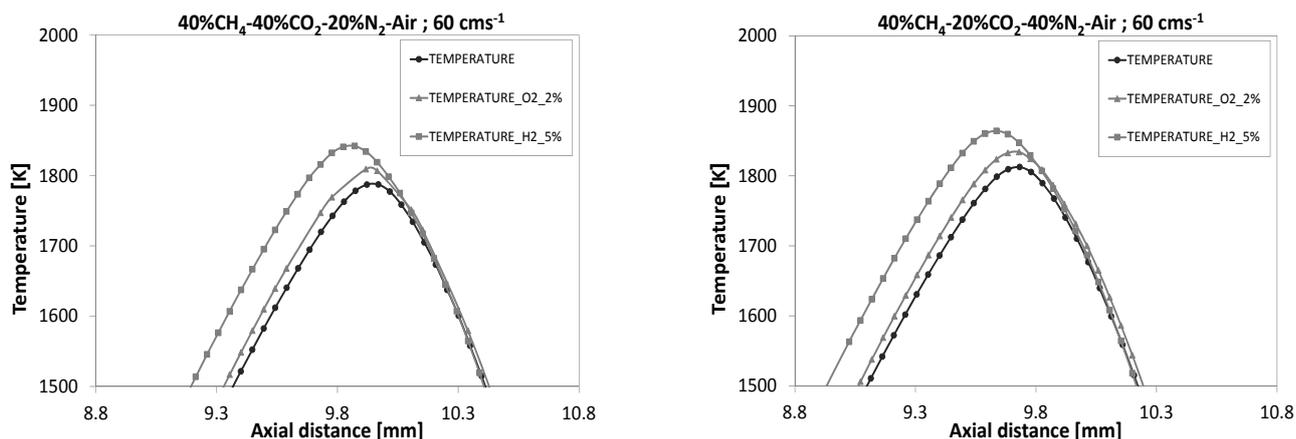


Fig. 4. Numerical solutions for temperature change in 40% CH<sub>4</sub> – 40% CO<sub>2</sub> – 20% N<sub>2</sub> – air (case A) flames with an addition of 2% O<sub>2</sub> or 5% H<sub>2</sub> at 60 cm s<sup>-1</sup> (left) and 40% CH<sub>4</sub> – 20% CO<sub>2</sub> – 40% N<sub>2</sub> – air (case B) flames with an addition of 2% O<sub>2</sub> or 5% H<sub>2</sub> at 60 cm s<sup>-1</sup> (right).

The modelled profiles of the Rayleigh scattering are being compared to the experimental ones measured for each flame. There is a good agreement between numerical and experimental results. When regarding the values for the differential scattering cross sections for the gases in these fuels [11] a factor of 2.38 can be derived between the cross sections of CO<sub>2</sub> and N<sub>2</sub>, this leading to the higher initial Rayleigh scattering on the fuel side (at axial distance 0–5.5 mm) for case A in comparison to case B. The initial Rayleigh scattering on the side of the oxidizer (at axial distance 13.8–18.9 mm) is equal in all cases, since air was introduced as oxidizer in all regarded studies. Towards the centre of the flame, where the peak temperatures are achieved, the scattering decreases markedly, due to the temperatures influence on the density of the gases.

The maximum temperatures at both 20 cm s<sup>-1</sup> and 60 cm s<sup>-1</sup> in case B decreased (21 K and 23 K respectively) compared to case A. This can be traced back to both a chemical [17] and a thermal effect [5], due to the modification of the diluent composition in the fuel and also because of the lower heat capacity and higher thermal diffusivity of N<sub>2</sub> compared to CO<sub>2</sub> as a diluent. As the velocities were increased in both cases A and B from 20 to 60 cm s<sup>-1</sup>, the peak temperatures decreased by 42 K and 40 K respectively, due to fewer radicals caused by shorter residence times, resulting in an incomplete flame chemistry. When increasing the velocity and therefore strain of the flame the diffusion process is limited, which leads to a shift of the flame towards the fuel side and simultaneously reduces the flames width.

Several quantities of O<sub>2</sub> (2, 4, 6, and 8% in volume) and 5% in volume of H<sub>2</sub> were added to the fuel side compositions for cases A and B. A small quantity of O<sub>2</sub> may appear in the product gas when using air as gasification agent during biomass gasification processes. The content of H<sub>2</sub> also varies strongly depending on the choice of agent.

An addition of 2% O<sub>2</sub> or 5% H<sub>2</sub> increased the peak temperatures by 1.5% and 3.5% respectively, despite the high fraction of CO<sub>2</sub> with a high heat capacity, according to the numerical results shown in Fig. 4. The peak temperatures of these highly diluted flames, being < 1850 K in all cases except case B without an addition, would possibly reduce a problem of thermal NO in combustion processes.

As stated the experimental determination of CH\* chemiluminescence at  $\lambda = 430$  nm is a simple method of detecting the region of maximum heat release and the exact physical position of the flame in order to predict unsteady combustion behaviour [18]. Concentration measurements of CH radicals are necessary for the spatial validation of flame models, as this radical exists in a thin high-temperature region [14]. The model calculates the CH radical concentration, as opposed to the experimental measurements, where the electronically excited CH\* radical is being measured. This led to continuously smaller peaks in the experimental solution, compared to the numerical outcome.

In both cases for the fuel-side compositions A and B, an increase of the velocities from 20 cm s<sup>-1</sup> to 60 cm s<sup>-1</sup> led to an increase of CH\* chemiluminescence peak intensities by 25–27%. Though fuel-side compositions with the higher proportion of CO<sub>2</sub> added as diluent results in consistently lower

levels of CH\* due to the quenching of the radicals by collision with the CO<sub>2</sub> molecule [19]. An addition of 2% O<sub>2</sub> or 5% H<sub>2</sub> by volume were also regarded for the velocity of 60 cm s<sup>-1</sup> in both cases. The O<sub>2</sub> addition led to an increase of 5.2% and 6.9% of CH\* for the compositions A and B respectively. The addition of H<sub>2</sub> resulted in an increase of 17.6% and 16.5% respectively. In case of O<sub>2</sub> this might be traced back to the reaction with the ethynyl radical, producing CH\* and therefore CO and CO<sub>2</sub> [20, 21]. An addition of H<sub>2</sub> to these hydrocarbon fuel mixes led to an increase of CH\* based on multiple formation reactions with C, CO and CHO [9].

Finally, the numerical results regarding the CH<sub>2</sub>O are shown in Fig. 5. CH<sub>2</sub>O is an important intermediate species in combustion, which is formed in preheating zones at the beginning of the flame front. Therefore, its presence is suited to

localize early stages of combustion. The left side of Fig. 5 shows the numerical results based on the fuel-side composition A at 20 cm s<sup>-1</sup> and 60 cm s<sup>-1</sup> without additives and the results with an addition of 2% O<sub>2</sub> or 5% H<sub>2</sub> to the fuel at 60 cm s<sup>-1</sup>. At higher velocity the addition of O<sub>2</sub> and especially H<sub>2</sub> led to a decrease in the CH<sub>2</sub>O mole fraction.

The addition of O<sub>2</sub> (up to 8%) resulted in the development of a premixed rich flame in the pre-chemistry zone (Fig. 5, right plot). The CH<sub>2</sub>O concentration increased markedly as the O<sub>2</sub> concentration increased and additionally, when raising the velocity and therefore the strain rate of the flame (a). This second flame was most prominent though at low strain (~130 s<sup>-1</sup>) and increasing O<sub>2</sub>. An addition of 8%, as opposed to 2%, O<sub>2</sub> here led to a difference in peak temperature of 100 K, markedly extending the flammability of the system, possibly leading to a more complete combustion.

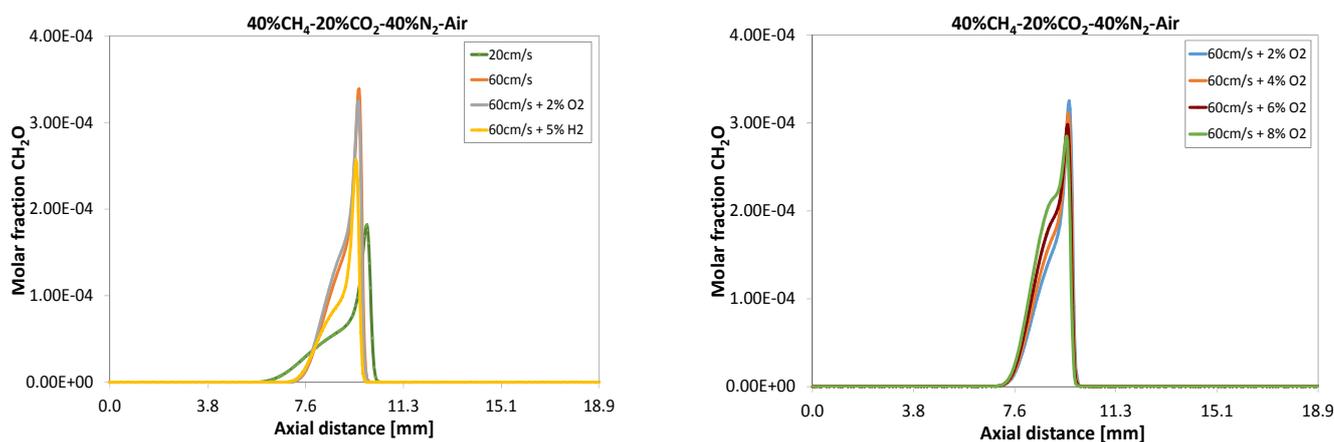


Fig. 5. Numerical results of formaldehyde molar fraction of 40% CH<sub>4</sub> – 20 % CO<sub>2</sub> – 40 % N<sub>2</sub> – air counter-flow flame at 20 cm s<sup>-1</sup> and 60 cm s<sup>-1</sup> (case A) and flames with an addition of 2% O<sub>2</sub> or 5% H<sub>2</sub> to the fuel-side at 60 cm s<sup>-1</sup> (left) and 40% CH<sub>4</sub> – 20% CO<sub>2</sub> – 40% N<sub>2</sub> – air flame 60 cm s<sup>-1</sup> with an addition of 2%, 4%, 6% and 8% of O<sub>2</sub> to the fuel-side (right).

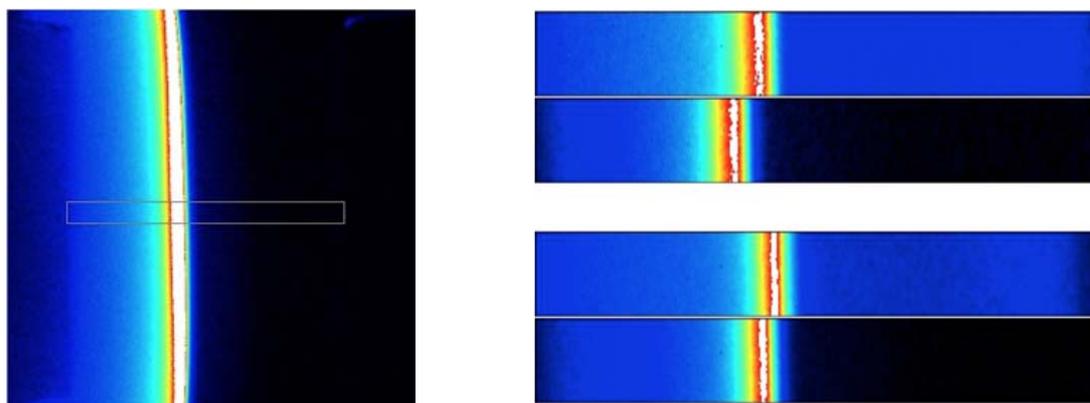


Fig. 6. Experimental CH\* chemiluminescence at  $\lambda_{CH^*} = 430$  nm from diluted non-premixed 40% CH<sub>4</sub> – 60% CO<sub>2</sub> – air flames; left figure: highlighted centreline of flames between nozzles with rectangle, 18.89 mm long, 45 pixels high (top: air side, bottom: fuel side), right figure top: flame at  $v_{air/fuel\ sides} = 20$  cm s<sup>-1</sup>,  $a = 41.1$  s<sup>-1</sup> with cold (top) and hot (bottom) nozzle on air side; right figure bot-tom: flame at  $v_{air/fuel\ sides} = 40$  cm s<sup>-1</sup>,  $a = 82.1$  s<sup>-1</sup> with cold (top) and hot (bottom) nozzle on air side.

Additionally, the influence of the N<sub>2</sub>-shroud flow (at 100% of the core jet velocities) and buoyancy effects due to a raise in temperature in the upper burner and a nozzle diameter of diameter < 25 mm were taken into account [22]. As shown in Fig. 6, the location of flames formed in a small burner (diameter = 24.7 mm) was greatly affected by buoyancy at low strains and increasing temperature. The change of temperature induced a change of the density at the oxidizer from the top nozzle. This buoyancy effect decreased at higher velocities and hence higher strain rates. The influence of the shroud flow and the buoyancy effect cannot be decoupled without further analysis [23].

#### 4. Conclusions

This study focused on the experimental and numerical investigations of complex gaseous mixtures, similar to the ones obtained in biomass gasification, with a high content of N<sub>2</sub> and CO<sub>2</sub> as diluents next to CH<sub>4</sub>, O<sub>2</sub> and H<sub>2</sub> as components. The investigations were carried out with counter-flow diffusion flames at low velocities and, therefore, strain. An increase of flow velocities and the thereby finally induced extinction of the diluted flames are discussed with respect to the changes of the temperature profiles and decreasing peak temperatures. Furthermore, with increasing strain rates a reduction of the flame width and the development of the CH<sub>2</sub>O concentration as well as of radicals like CH\* were analysed.

The experimental laser-induced Rayleigh scattering and the subsequently following temperature distributions were in good agreement with the numerical results. The proportions of different diluents in the composition on the fuel-side led to differing results regarding the peak temperatures at varying velocities, mostly resulting from chemical and thermal effects, based on heat capacities and thermal diffusivities. Small quantities of H<sub>2</sub> and O<sub>2</sub> had a considerable effect, not only on peak temperatures in all flames considered, but also on the molar fractions and signal intensities of CH\* and CH<sub>2</sub>O, which were also in good agreement for both the numerical and the experimental studies. The choice of the diluent also played a major role, especially with respect to flame resilience to extinction by strain. Lastly, an addition of O<sub>2</sub> to the fuel in smaller quantities had a great impact on the formaldehyde concentration and expanded the flammability of the system markedly with respect to strain. This would advance the possibility of the

introduction of air to i.e. a gasification system, as a cheap solution for a more complete combustion system.

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